

DOI: 10.21767/2349-3917.100030

Detecting tāla Computationally in Polyphonic Context-A Novel Approach

Susmita Bhaduri*, Anirban Bhaduri and Dipak Ghosh,

Deepa Ghosh Research Foundation, Maharaja Tagore Road, India

*Corresponding author: Susmita Bhaduri, Deepa Ghosh Research Foundation, Maharaja Tagore Road, India, Tel: 919836132200; E-mail: susmita.sbhaduri@gmail.com

Received Date: October 01, 2018; Accepted Date: October 04, 2018 Published Date: October 29, 2018

Citation: Bhaduri S, Bhaduri A, Ghosh D (2018) Detecting tāla Computationally in Polyphonic Context-A Novel Approach. Am J Compt Sci Inform Technol Vol.6 No.3: 30

Copyright: ©2018 Bhaduri S, et al. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

Abstract

In North-Indian-Music-System (NIMS), *tablā* is mostly used as percussive accompaniment for vocal-music in polyphonic-compositions. The human auditory system uses perceptual grouping of musical-elements and easily filters the *tablā* component, thereby decoding prominent rhythmic features like *tāla*, tempo from a polyphonic-composition. For Western music, lots of work has been reported for automated drum analysis of polyphonic-composition. However, attempts at computational analysis of *tāla* by separating the *tablā*-signal from mixed signal in NIMS have not been successful. *Tablā* is played with two components-right and left. The right-hand component has frequency overlap with voice and other instruments. So, *tāla* analysis of polyphonic-composition, by accurately separating the *tablā*-signal from the mixture is a baffling task, therefore an area of challenge. In this work we propose a novel technique for successfully detecting *tāla* using left-*tablā* signal, producing meaningful results because the left-*tablā* normally doesn't have frequency overlap with voice and other instruments. North-Indian-rhythm follows complex cyclic pattern, against linear approach of Western-rhythm. We have exploited this cyclic property along with stressed and non-stressed methods of playing *tablā*-strokes to extract a characteristic pattern from the left-*tablā* strokes, which, after matching with the grammar of *tāla*-system, determines the *tāla* and tempo of the composition. A large number of polyphonic (vocal+*tablā*+other-instruments) compositions has been analyzed with the methodology and the result clearly reveals the effectiveness of proposed techniques.

framework. We should consider a knowledge-based approach to create the computational model for NIMS rhythm. Tools developed for rhythm analysis can be useful in a lot of applications such as intelligent music archival, enhanced navigation through music collections, content based music retrieval, for an enriched and informed appreciation of the subtleties of music and for pedagogy. Most of these applications deal with music compositions of polyphonic kind in the context of blending of various signals arising from different sources. Apart from the singing voice, different instruments are also included.

As per rhythm relates to the patterns of duration that are phenomenally present in the music [1]. It should be noted that that these patterns of duration are not based on the actual duration of each musical event but on the Inter Onset Interval (IOI) between the attack points of successive events. As per Grosvenor et al., an accent or a stimulus is marked for consciousness in some way [2]. Accents may be phenomenal, i.e. changes in intensity or changes in register, timbre, duration, or simultaneous note density or structural like arrival or departure of a cadence which causes a note to be perceived as accented. It may be metrical accent which is perceived as accented due to its metrical position [3]. Percussion instruments are normally used to create accents in the rhythmic composition. The percussion family which normally includes timpani, snare drum, bass drum, cymbals, triangle, is believed to include the oldest musical instruments, following the human voice [4]. The rhythm information in music is mainly and popularly provided by the percussion instruments. One simple way of analyzing rhythm of a composite or polyphonic music signal having some percussive component, may be to extract the percussive component from it using some source separation techniques based on frequency based filtering. Various attempts have been made in Western music to develop applications for re-synthesizing the drum track of a composite music signal, identification of type of drums played in the composite signal (ex. the works of Gillet et al. and Nobutaka et al. etc., described in the below section in detail) [5,6]. Human listeners are able to perceive individual sound events in complex compositions, even while listening to a polyphonic music recording, which might include unknown timbres or musical instruments. However designing an

Keywords: Left-*tablā* drum; *Tāla* detection; Tempo detection; Polyphonic composition; Cyclic pattern; North Indian Music System-NIMS

Introduction

Current research in Music-Information-Retrieval (MIR) is largely limited to Western music cultures and it does not address the North-Indian-Music-System hereafter NIMS, cultures in general. NIMS raise a big challenge to current rhythm analysis techniques, with a significantly sophisticated rhythmic

automated system for rhythm detection from a polyphonic music composition is very difficult.

In this work we propose an absolutely novel approach of detecting *tāla* from classical and semi classical North Indian polyphonic music compositions. The rest of the paper is organized as follows. Some relevant definitions of North-Indian-Music-System (NIMS) are provided in definitions. A review of past work is presented in the novelty of proposed method and further research details are elaborated in the respective section.

Definitions

Tāla and its structure in NIMS

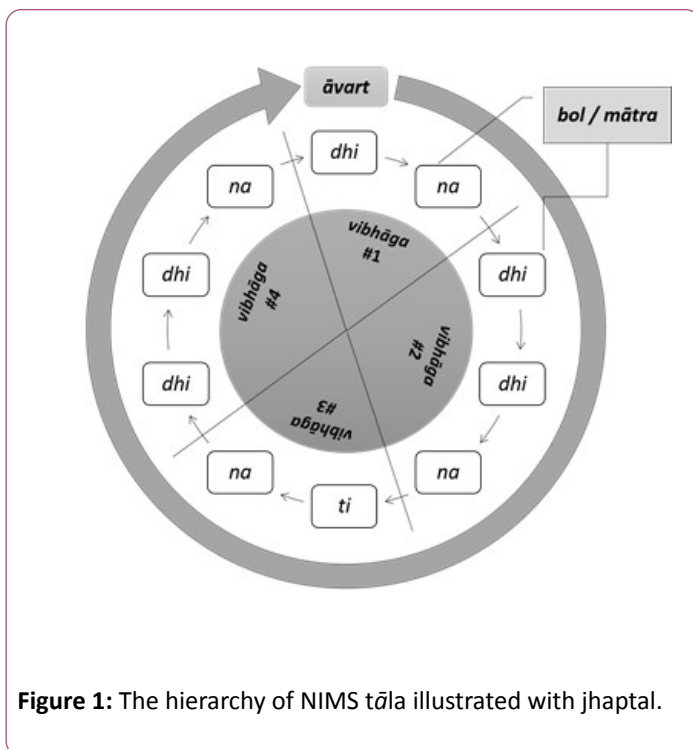


Figure 1: The hierarchy of NIMS tāla illustrated with jhaptal.

The basic identifying features of rhythm or *tāla* in NIMS are described as follows.

Tāla and its cyclicity: North Indian music is metrically organized and it is called nibaddh (bound by rhythm) music. This kind of music is set to a metric framework called *tāla*. Each *tāla* is uniquely represented as cyclically recurring patterns of fixed time-lengths.

āvart: This recurring cycle of time-lengths in a *tāla* is called *āvart*. *vart* is used to specify the number of cycles played in a composition, while annotating the composition.

Mātra: The overall time-span of each cycle or *āvart* is made up of a certain number of smaller time units called *mātra*-s. The number of *mātra*-s for the NIMS *tāla*-s, usually varies from 6 to 16.

Vibhāga: The *mātra*-s of a *tāla* are grouped into sections, sometimes with unequal time-spans, called *vibhāga*-s.

• **Bol:** In the *tāla* system of North Indian music, the actual articulation of *tāla* is done by certain syllables which are the

mnemonic names of different strokes/pulses corresponding to each *mātra*. These syllables are called *bol*-s. There are four types of *bol*-s as defined below.

- **Sam:** The first *mātra* of an *āvart* is referred as *sam* which is mandatorily stressed [7].
- **Tāli-bol:** *Tāli*-*bol*-s are usually stressed, whereas *khāli*-s are not. *Tāli* -*bol*-s are gestured by the *tablā* player with claps of the hands, hence are called *sasabda kriya*. The *sam* is almost always a *Tāli*-*bol* for most of the *tāla*-s, with only exception of *rupak tāla* which designates the *sam* with a moderately stressed *bol* called *khali* (as explained below) [8]. Highly stressed *vibhāga* boundaries are indicated through the *tāli*-*bols* [8]. *Tāli*-*sam* is indicated with a (+) in the rhythm notation of NIMS. Consequent *Tāli*-*vibhāga*-boundaries are indicated with 2,3...
- **Khali-bol:** *Khali* literally means empty and for NIMS it implies wave of the hand or *nisabda kriya*. Moderately stressed *Vibhāga* boundaries are indicated through the *khali*-*bols* so we almost never find the *khali* applied to strongly stressed *bol*-s like *sam* [8]. *Khali*-*sam* is indicated with a (0) in the rhythm notation of NIMS and consequent *khali*-*vibhāga*-boundaries are indicated also with 0.
- **Absent-bol:** Sometimes while playing *tablā*, certain *bol*-s are dropped maintaining the perception of rhythm intact. They are called rests and they have equal duration as a *bol*. We have termed them as absent strokes/*bol*-s. These *bol*-s are denoted by (*) in the rhythm notation of a NIMS composition Ancient-future. In the Figure 2, the waveform of absent *bol*, denoted by (*), is shown just after another *bol* *ta*, played in a *tablā*-solo. Normally in a NIMS composition there may be many absent *bol*-s in the *thekā* played for the *tāla*. In these cases other percussive instruments (other than *tablā*) and vocal emphasis might generate percussive peaks for the time positions of the absent strokes, depending on the composition, the lyrics being sung and thus the rhythm of the composition is maintained.

Thekā: For *tablā*, the basic characteristic pattern of *bol*-s that repeats itself cyclically along the progression of the rendering of *tāla* in a composition, is called *thekā*. In other words it's the most basic cyclic form of the *tablā* [8]. Naturally *thekā* corresponds to the basic pattern of *bol*-s in an *āvart*. The strong starting *bol* or *sam* along with the *tāli*-*vibhāga*-boundaries in a *thekā* carries the main accent and creates the sensation of cadence and cyclicity.

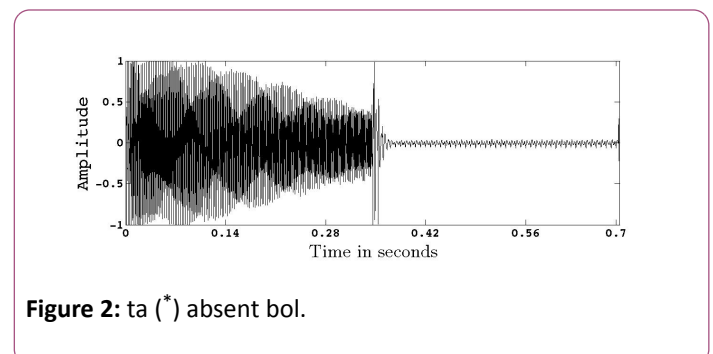


Figure 2: *ta* (*) absent *bol*.

Description of the definitions with an example: The details of these theories are shown in the structure of a *tāla*, called *jhaptal*

in the Table 1 and Figure 1. The hierarchy of the features and their interdependence are shown in the Figure 1. The cyclic property of tāla is evident here.

Table 1: Description of jhaptal, showing the structure and the its basic bol-pattern or the thekā

tā li	+		2			0		3		
bol	Dhi	na	dhi	dhi	Na	ti	na	dhi	dhi	na
mātrā	1	2	3	4	5	6	7	8	9	10
vibhāga	1		2			3		4		
āvart	1									

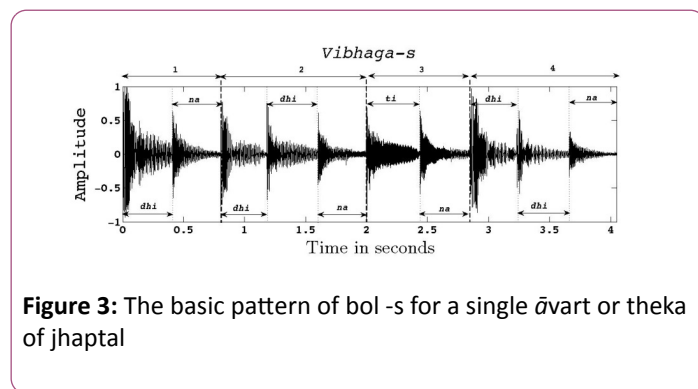


Figure 3: The basic pattern of bol -s for a single āvart or theka of jhaptal

- The first row of Table 1 shows the sequence of tali-s and the khali-s in a thekā or āvart of jhaptal. In this row the sam is indicated with a (+) sign and it should be noted that for jhaptal it is a tali-bol. The second tāli-vibhāga-boundary is denoted by (2) followed by a (0) as it is the first khali-vibhaga-boundary and then by one more tali denoted by (3) in a single cycle or thekā.
- The amplitude waveform of the same thekā is shown in the Figure 3. The sam is shown in the Figure as the first bol dhi. This clip of jhaptal is available in Tabla Radio.
- The second row of the Table 1 shows the bol-s of jhaptal in its thekā. In the Figure 3 the waveform of all these bol-s of a single cycle of jhaptal are shown.

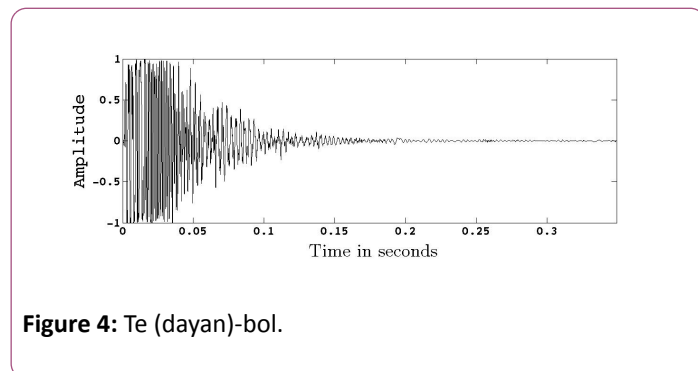


Figure 4: Te (dayan)-bol.

- Jhaptal thekā comprises of ten mātrā -s which are shown as per their sequence in third row of Table 1.
- In the fourth row of the Table 1, the section or vibhāga-boundary-positions and sequences are shown. These vibhāga-sequences are shown for jhaptal in the Figure 3. We can see that there are four vibhāga-s in jhaptal theka and

first vibhāga-boundary is a tāli-sam-bol dhi having mātrā number as one. Second vibhāga-boundary is again tāli-bol dhi having mātrā number as three and so on.

In the fourth row of the Table 1, āvart-position and sequence is shown. As there is one cycle shown so āvart-sequence is 1.

Tablā and bol-s

Tablā, the traditional percussive accompaniment of NIMS, consists of a pair of drums. Bayan the left drum, is played by the left hand and made with metal or clay. It produces loud resonant or damped non-resonant sound. As bayan cannot be tuned significantly, when it is played, it produces a fixed range of frequencies. The dayan is the wooden treble drum, played by the right hand. A larger variety of acoustics is produced on this drum when tuned in different frequency ranges. In the tāla system of North Indian music, the representation of tāla is done mainly by playing bol-s on the tablā. bol-s as they are played in tablā are listed in Table 2. Figure 4, Figure 5 and Figure 6 shows the waveform of few sample waveforms of the bol-s te, dha and ge respectively. The clip of the bol-s are taken from Tabla Radio

Table 2: List of commonly played bol-s in either on bayan or dayan or together on both.

played on bayan	played dayan	on played on both bayan and dayan
ke, ge, ghe, kath	na, tin, tun, ti, te, ta, da	dha (na+ge), dhin (tin+ge), dhun (tun+ge), dhi (ti+ge)

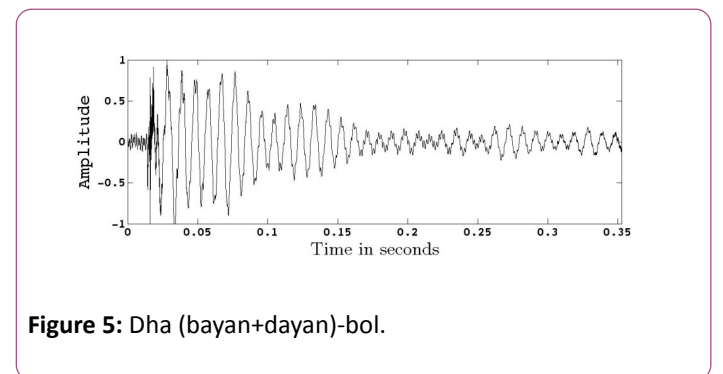


Figure 5: Dha (bayan+dayan)-bol.

Most of the tāla-s have tāli-sam played either with bayan alone or with bayan and dayan played simultaneously [8]. Same thing happens for the tāli-vibhāga boundaries. Most of the North Indian classical, semi-classical, devotional and popular songs are played as per the tāla-s in Table 3. The most commonly played thekā-s are shown in this Table, Ref. Tabla Class; TAALMALA-THE RHYTHM OF MUSIC. For our experiment, we have considered the thekā-s listed in the Table 6 for the tāla-s dadra, kaharba, rupak and bhajani. For these thekā-s, the stressed bol-s having a bayan component is shown in bold and pipes in bold indicate vibhāga boundary.

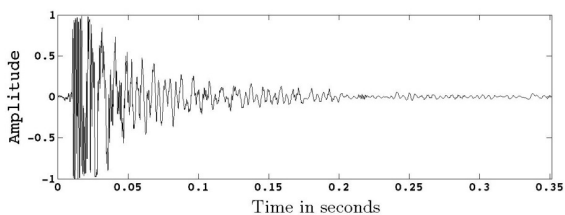


Figure 6: Ge (bayan)-bol.

It is evident from the Table 3 that all the *tāla*-s except *rupak*, start with a *tali-sam-bol* having both *dayan* and *bayan* component. Only *rupak* starts with a *khali-sam* and its *sam* does not contain any *bayan* component. *Bhajani tāla*, is often played with a variation for *bhajan*, *kirtan* or *qawwali* songs [9], which makes the first (*tali-sam*) and fourth *bol* as stressed. Although this fourth *bol* is not a *tali vibhaga* boundary still it is rendered as stressed and it is to be noted here that this *bol* is played with

dayan and *bayan* together. We have considered this *bhajani theka* with first (*tali-sam*) and fourth *bol* as stressed, because data in our experiment includes popular *bhajan* or devotional compositions.

For the *tāla*-s *dadra* and *kaharba* the number of pulses in the *theka* and the *matra*-s are identical but for *rupak* and *bhajani* each *matra* is divided in to two equal duration *bol*-s. In effect *rupak* is a 7 *mātrā tāla* but has 14 pulses or *bol*-s and *bhajani* is 8 *mātrā tāla* but has 16 pulses or *bol*-s. *Bhajani thekā* in the Table 3 has half of its number of strokes as absent *bol*-s or rests (denoted by *).

It should be noted that the standard *thekā* of *rupak* is *tin|tin|tin|na|dhin|na|dhin|na*, but we have taken another *thekā* shown in the Table 3 for our experiment Refer *Gurbani*. This *thekā* is normally followed for the semi-classical soundtracks and popular hindi songs. Moreover, we got maximum number of annotated samples of polyphonic songs composed with this *thekā* for our validation process.

Table 3: Table of popular *thekā*-s of North Indian rhythms.

<i>tāla</i>	Number of <i>mātrā</i> -/ <i>vibhā ga</i> in an <i>āvart</i>	<i>thekā</i>
<i>dadra</i>	3 3	<i>dha dhi na na ti na</i>
<i>kaharba</i>	4 4	<i>dha ge na ti na ke dhi na</i>
<i>rupak</i>	3 2 2	<i>tun na tun na ti te dhin dhin dha dha dhin dhin dha dha</i>
<i>bhajani</i>	4 4	<i>dhin*na dhin*dhin na* tin*na tin*tin na*</i>
<i>jhaptal</i>	2 3 2 3	<i>dhi na dhi dhi na ti na dhi dhi na</i>
<i>tintal</i>	4 4 4 4	<i>dha dhin dhin dha dha dhin dhin dha na tin tin na te-Te dhin dhin dha</i>

Lay or tempo

An important concept of rhythm in NIMS is *lay*, which governs the tempo or the rate of succession of *tāla*. The *lay* or tempo in NIMS can vary among *ati-vilambit* (very slow), *vilambit* (slow), *madhya* (medium), *ḍrūta* (fast) to *ati-ḍrūta* (very fast). Tempo is expressed in beats per minute or BPM.

Based on the definitions of the current section a detailed survey of the previous works in the rhythm analysis area both in Western and Indian music is elaborated in the following section.

Past work

Although various rhythm analysis activities have been done for Western music, not much significant work has been done in the context of NIMS. Although the rhythmic aspect of Western music is much simpler in comparison to Indian one, to get the broad idea of the problem, our study includes the work on Western music. The extraction of percussive events from a polyphonic composition is an ongoing and challenging area of research. We have discussed existing drum separation approaches in Western music in 4, as they are relevant to our methodology. The existing works in meter analysis and beat-tracking for Western music, are discussed in the following

section. Then similar discussion is made on existing rhythm analysis works in Indian music.

Meter analysis in Western music

In Western music beats have sharp attacks, fast decays and are uniformly repeated while in Middle Eastern and Indian music beats have irregular shapes. This is due the fact that bass instruments in these cultures are different from what is used in Western bands. By examining the distribution of Western meters, Alghoniemy and Tewfik found that they deviate from Gaussianity by a larger amount than non-western meters [10].

Works have been done by parsing MIDI data into rhythmic levels by Rosenthal et al. [11]. But that cannot deal real audio data, attempted to encode the musical texts, notes into sequence of numbers and \pm signs [12]. But it can be implemented only for the Western compositions for which the notation is available.

Todd and Brown [13] showed multi-scale mechanism for the visualization of rhythm as rhythmogram. The rhythmogram provides a representation to the structure of spoken words and poems used, which is very different from polyphonic music but the model is implemented on synthesized binary pattern, strong and weak pulses, not from actual music composition.

Alghoniemy and Tewfik [10] analysed the beat and rhythm information with a binary tree or trellis tree parsing depending on the length of the pauses in the input polyphonic signal. The approach relies on beat and rhythm information extracted from the raw data after low-pass filtering. It has been tested using music segments from various cultures.

Foote et al. [14], described methods for automatically locating points of significant change in music or audio, by analysing local self-similarity. This approach uses the signal to model itself, and thus does not rely on particular acoustic cues nor requires training.

Klapuri and Astola [15] describes a method of estimating the musical meter jointly at three metrical levels of measure, beat and subdivision, which are referred to as measure, tactus and tatum, respectively. For the initial time-frequency analysis, a new technique is proposed which measures the degree of musical accent as a function of time at four different frequency ranges. This is followed by a bank of comb filter resonators which extracts features for estimating the periods and phases of the three pulses. The features are processed by a probabilistic model which represents primitive musical knowledge and uses the low-level observations to perform joint estimation of the tatum, tactus, and measure pulses.

Gouyon and Herrera [16] addressed the problem of classifying polyphonic musical audio signals of Western music, by their meter, whether duple/triple. Their approach aimed to test the hypothesis that acoustic evidences for downbeats can be measured on signal low-level features by focusing especially on their temporal recurrences.

Beat-tracking in Western music

In the work of Bhat [17], a beat tracking system is described. A global tempo is first estimated. A transition cost function is constructed based on the global tempo. Then dynamic programming is used to find the best-scoring set of beat times that reflect the tempo.

In Goto and Muraoka [18] a real-time beat tracking system is designed, that processes audio signals that contain sounds of various instruments. The main feature of this work is to make context-dependent decisions by leveraging musical knowledge represented as drum patterns

In Scheirer [19], the envelope of the music signal is extracted at different frequency bands. The envelope information is then used to extract and track the strokes/pulses.

To classify percussive events embedded in continuous audio streams, [20] relied on a method based on automatic adaptation of the analysis frame size to the smallest metrical pulse, called the tick.

Dixon [21] has created a system named Beat Root for automatic tracking and annotation of strokes for a wide range of musical styles. Davies and Plumbley [22] proposed a context dependent beat tracking method which handles varying tempos by providing a two state model. The first state tracks the tempo changes, then the second maintains contextual continuity within a single tempo hypothesis. Böck et al. [23] proposed a data

driven approach for beat tracking using context-aware neural networks.

Rhythm analysis in Indian Music

The concepts of *tāla* and its elements are briefed in above section. For Indian percussive systems, strokes are of irregular nature and mostly are not of same strength. In comparison with Western music, not much significant work in rhythm analysis in Indian music has been reported so far.

Rhythm analysis and modeling for Indian music can be traced back to the study of acoustics of Indian drums by Sir C. V. Raman. In this work, the importance of the first three to five harmonics which are derived from the drum-head's vibration mode was highlighted. In the last decade, most of the MIR research on Indian music rhythm has been focused on drum stroke transcription, creative modeling for automatic improvisation of *tablā* and predictive modeling of *tablā* sequences. Bhat [17] extended Raman's work and to explain the presence of harmonic overtones, he applied a mathematical model of the vibration modes of the membrane of a type of Indian musical drum called *mridanga*. Goto and Muraoka [18] were first to achieve a reasonable accuracy for tempo analysis on audio signals operated in real time. Their system was based on agent based architecture and tracking competing meter hypotheses. Malu and Siddharthan [25] confirmed C.V. Raman's conclusions on the harmonic properties of Indian drums, and the *tablā* in particular. They accredited the presence of harmonic overtones to the central black patch of the *dayan*. Patel et al. [26] performed an acoustic and perceptual comparison of *tablā bol-s* (both, spoken and played). They found that spoken *bol-s* have significant correlations with played *bol-s*, with respect to acoustic features like spectral flux, centroid etc. It also enables untrained listeners to match the drum sound with corresponding syllables. This gave strong support to the symbolic value of *tablā bol-s* in North Indian drumming tradition.

Gillet et al. [5] worked on *tablā* stroke identification. Their approach had three steps: stroke segmentation, computation of relative durations (using beat detection techniques), and stroke recognition, after which they used the Hidden Markov Model (HMM) for transcription. But their work is mostly intended for rhythm transcription. Gouyon and Herrera [16] suggested a method to detect rhythm type, where the beat indices are manually extracted and then an autocorrelation function is computed on selected low level features like-spectral flatness, energy flux, energy in upper half of the first bark band. This helped in the advancing the beat-tracking algorithms.

State of the Art Works: The system proposed by Rae uses Probabilistic Latent Component Analysis method to extract *tablā* signals from polyphonic *tablā solo* [27]. Then each separated signal is re-synthesized in each layer and the music is regenerated in *quida* (improvisation of *tablā* performances) model. The work is restricted to *tablā solo* performances where the *tablā* signal is the most significant component, and not for polyphonic compositions where *tablā* is one of the percussive accompaniment.

In Gulati and Rao the work of Schuller et al. is extended [28,29]. The methodology for meter detection in Western music is applied for Indian music. A two-stage comb filter-based approach, originally proposed for double/triple meter estimation, is extended to a septuple meter (such as 7/8 time-signature). But this model does not conform to the *tāla* system of Indian music.

Miron [30] explored various techniques for rhythm analysis based on the Indian percussive instruments. An effort is made to extract the *tablā* component from a polyphonic music by estimating the onset candidates with respect to the annotated onsets. Various existing segmentation techniques for annotating polyphonic *tablā* compositions, were also tried. But the goal of automatic detection of *tāla* in Indian music did not succeed.

Some work has been done to detect a few important parameters like *mātrā*, tempo by first using signal level properties and then using cyclic properties of *tāla*. The work in Bhaduri et al. [31] for *mātrā* and tempo detection for NIMS *tāla*-s, is based on the extraction of beat patterns that get repeated in the signal. Such pattern is identified by processing the amplitude envelope of a music signal. *Mātrā* and tempo are detected from the extracted beat pattern. This work is extended to handle different renderings of the *kekā*-s comprised of single and composite *bol*-s. In this work Bhaduri et al. [32] *bol* duration histogram is plotted from the beat signal and the highest occurring *bol*-duration is taken as the actual *bol*-duration of the input beat signal. The above methodology has been tested on electronic *tablā* signal. In case of the real *tablā* signal it is impossible to maintain consistency in terms of the periodicity of the *bol*-s or beat-s played by a human. To resolve this issue the work is further extended and modified to handle real *tablā* signal and this comparison is carried out for the entire beat signal and a weight-age or the probability of the experimental signal being played according to certain *tāla*-s of NIMS, is calculated [33]. The *mātrā* of the *tāla* for which this weightage is maximum, is confirmed as the *mātrā* of the input signal. This methodology was tested with real-*tablā*-solo performance recordings. In recent times experiments and analysis have been done with non-stationary, nonlinear aspects of NIMS [34].

It is evident from the study that rhythm analysis in NIMS, focusing on *tāla* rendered with *tablā*, the most popular North Indian percussive instrument, is a wide area of research. In our work, an approach for rhythm analysis is proposed, which is built around the theory of *tāla* in NIMS. On the background of the past works in the related field, the novelty of our approach is elaborated in the following section.

The Novelty of the Proposed Method

In the context of NIMS rhythm popularly known as *tāla*, *tablā* is the most popular percussive instrument. Its right hand drum-*dayan* and left hand drum-*bayan* are played together and amplitude-peaks spaced at regular time intervals, are created by playing every stroke. One way of rhythm information retrieval from polyphonic composition having *tablā* as one of the percussive instruments, may be to extract the *tablā* signal from it and analyze it separately. The *dayan* has a frequency overlap

with other instruments and mostly human-voice for polyphonic music, so if we extract the whole range of frequencies for both *bayan* and *dayan* components, by existing frequency based filtering methods, the resultant signal will be a noisy version of original song as it will still have part of other instruments, human voice components along with *tablā*. Also conventional source separation methods lead to substantial loss of information or sometimes addition of unwanted noise. This is the an area of challenge in *tāla* analysis for NIMS. Although, NIMS *tāla* functions in many ways like Western meter, as a periodic, hierarchic framework for rhythmic design, it is composed of a sequence of unequal time intervals and has longer time cycles. Moreover *tāla* in NIMS is distinctively cyclical and much more complex compared to Western meter [35]. This complexity is another challenge for *tāla* analysis.

Due to the above reasons defining a computational framework for automatic rhythm information retrieval for North Indian polyphonic compositions is a challenging task. Very less work has been done for rhythmic information retrieval from a polyphonic composition in NIMS context. In Western music, quite a few approaches are followed for this purpose, mostly in the areas of beat-tracking, tempo analysis, annotation of strokes/pulses from the separated percussive signal. We have described these systems above. For NIMS, very few works of rhythm analysis are done by adopting Western drum-event retrieval system. These works result in finding out meter or speed which are not very significant in the context of NIMS. Hence this is an unexplored area of research for NIMS.

In this work we have proposed a completely new approach, i.e. instead of extracting both *bayan* and *dayan* signal, we have extracted only the *bayan* signal from the polyphonic composition by using band-pass filter. This filter extracts lower frequency part which normally does not overlap with the frequency of human voice and other instruments in a polyphonic composition. Most of the *tāla*-s start with a *bol* or stroke which has a *bayan* component (either played with *bayan* alone or both *bayan* and *dayan* together) and also the some consequent section (*vibhāga* in NIMS terminology) boundary-*bol*-s have similar *bayan* component. Hence these strokes would be captured in the extracted *bayan* signal. For a polyphonic composition, its *tāla* is rendered with cyclically recurring patterns of fixed time-lengths. This is the cyclic property of NIMS, discussed in detail in the above section. So after extracting the starting *bol*-s and the section boundary strokes from the *bayan* signal, we can exploit the cyclic property of a *tāla* and the pattern of strokes appearing in a single cycle and can detect important rhythm information from a polyphonic composition. This would be a positive step towards rhythm information retrieval from huge collection of music recordings for both film music and live performances of various genres of hindi music. Here, we consider the *tāla* detection of different single-channel, polyphonic clips of Hindi vocal songs of devotional, semi-classical and movie soundtracks from NIMS, having variety of tempo and *mātrā*-s.

Proposed Methodology

As it has been already discussed that there is a frequency overlap between *tablā* (bayan and dayan) with voice and other instruments in a polyphonic composition, accurate extraction of *tablā* signal from the mixed signal by following the source separation techniques based on frequency based filtering has not been very successful [36,37]. Also these source separation methods lead to substantial loss of information or sometimes addition of unwanted noise. It has motivated us to look for an alternate approach. Here we have adopted a four-step methodology which is detailed out in following sections.

- First we have processed the polyphonic input signal by partially adopting a filter-based separation technique. In doing so we are able to separate out the bayan-stroke-signal which would consist of the only bayan-strokes and also the bayan-components of bayan+dayan-strokes.
- Then further, we have processed the entire polyphonic signal and generated a peak-signal, which comprises of all the emphasized peak-s generated out of *tablā* and other percussive instruments played in the polyphonic composition of a specific *tāla*. Peak-signal would contain the peak-s of bayan-stroke-signal, and also the emphasized peak-s of *tablā* (i.e. only dayan -strokes and bayan+dayan-strokes). If other percussive instruments played, then in addition to the above, the peak-signal would also contain emphasized peak-s generated out of them
- Next we have refined the bayan-stroke-signal and the peak-signal.
- Lastly we propose to generate a co-occurrence matrix from both kinds of signals and exploit domain specific information of *tablā* and *tāla* theory, to detect the *tāla* and tempo of the input polyphonic signal.

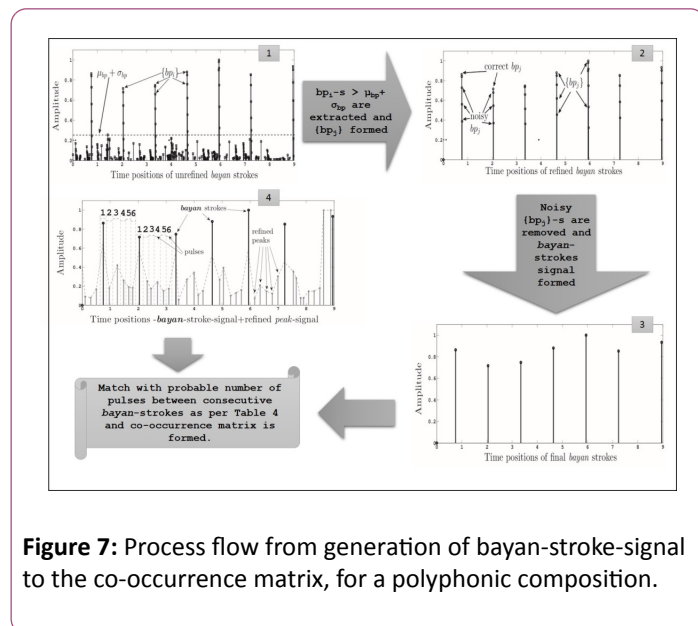


Figure 7: Process flow from generation of bayan-stroke-signal to the co-occurrence matrix, for a polyphonic composition.

Overall flow of the process starting from generation of bayan-stroke-signal to the final co-occurrence matrix is shown in the Figure 7, for a test clip composed in *dadra tāla*. The process of

generating final bayan-stroke-signal [sub-figure 3] and final peak-signal [sub-figure 4] are described.

Separation of *bayan-stroke-signal*

In Western music drum is one of the mostly used percussive instruments. Extraction of drum signal is a part of applications like identification of type of drums, re-synthesizing the drum track of a composite music signal. Existing approaches for drum signal separation and our method of extracting bayan-stroke-signal is described at various sections.

Drum separation approaches in Western music:

- **Blind Source Separation method:** Christian Uhle, Christian Dittmar, Thomas Sporer [36] proposed a method based on Independent Subspace Analysis method to separate drum tracks from popular Western music data. In the work of Helén and Virtanen [37], a method has been proposed for the separation of pitched musical instruments and drums from polyphonic music. Non-negative Matrix Factorization (NMF) is used to analyze the spectrogram and thereby to separate the components.
- **Match and adapt method:** The methodology defines the template (temporal as stated in [38] or spectral as stated in [39], of drum sound, then searches for similar patterns in the signal. The template is updated and also improved in accordance with those observations of patterns. This set of methods extracts as well as transcripts drum component.
- **Discriminative model:** This approach is built upon a discriminative model between harmonic and drums sounds. In the work of Gillet and Richard [40], music signal is split into several frequency bands, the for each band the signal is decomposed into deterministic and stochastic part. The stochastic part is used to detect drum events and to re-synthesize a drum track. Possible applications include drum transcription, remixing, and independent processing of the rhythmic and melodic components of music signals. Ono et al [6] have proposed a method that exploits the differences in the spectrograms of harmonic and percussive components.

Our approach: Our approach for separating out bayan-stroke-signal falls in the Discriminative model group for separating out harmonic and drums sounds, among the three categories described above.

To extract the bayan-stroke-signal we have used ERB or Equivalent Rectangular Bandwidth filter banks. The ERB is a measure used in psychoacoustics, which gives an approximation to the bandwidths of the filters in human auditory system [41]. Alghoniemy and Rosenthal [10] have done empirical study of western drums and confirmed that that they could extract the bass drum sequences by filtering the music signal with a narrow bandpass filter. Ranade [42] confirmed the same range (60-200 Hz) for the bass drum or bayan of Indian *tablā* . If we take ERB filter banks to extract different components like voice, *tablā* and other accompaniments from the polyphonic signal with sampling rate of 44100 Hz, the central frequency of the second bank comes out to be around 130 Hz and the bandwidth of around 60-200 Hz. It has been observed from the spectral and

wavelet analysis of the different type of bayan-bol-s and Table 2 that their frequency ranges around the same central frequency and bandwidth. So we have divided the input polyphonic signal sampled at 44100Hz, into 20 ERB filter banks and extracted the second bank for constructing the bayan-stroke-signal. We have used MIRtoolbox to extract this frequency range from ERB filter banks.

As described earlier, most of the *tāla* -s in NIMS start with a highly stressed *tāla*-sam-bol played with bayan or bayan and dayan combined. Moreover *tāla* vibhāga boundaries are also usually stressed. Thus extracted bayan-stroke-signal would mostly consist of peak-s generated from *tāla*-sam-s and *tāla*-vibhāga boundaries. There might be presence of other high-strength-peak-s generated out of bol-s having bayan component, other than *tāla*-sam and *tāla*-vibhāga boundaries, for compositions with slow (20BPM) or very slow (10BPM) tempo. But for popular, semi-classical and filmy North Indian compositions, the tempo is moderate to fast. These compositions mostly do not have the emphasized, high strength bayan-peak-s other than *tāla*-sam, *tāla*-vibhāga boundaries in the bayan-stroke-signal. Even if these additional bol-s having bayan-component, produce peak-s in the bayan-stroke-signal, their strength is much weaker, compared to *tāla*-sam or *tāla*-vibhāga boundaries.

The process below is followed to remove these additional bol-s having bayan component, from the bayan-stroke-signal.

- Let $\{bp_i\}$ be the set of peak-s in the bayan-strokes-signal extracted from a polyphonic song-signal. Please note the Figure Figure 7(1), where $\{bp_i\}$ -s for a particular polyphonic sample of dadra *tāla* are shown.
- We calculate the mean $-\mu_{bp}$ and standard deviation $-\sigma_{bp}$ for the set $\{bp_i\}$. In the Figure 7 (1), the corresponding value of $\mu_{bp}+\sigma_{bp}$ is shown. It should be noted there are lots of noisy peak-s with magnitude less than $\mu_{bp}+\sigma_{bp}$.

- $\{bp_j\}$ is obtained as a subset of $\{bp_i\}$ after selecting the high-strength bayan-strokes greater than $\mu_{bp}+\sigma_{bp}$.
- $\{bp_j\}$ is the set of strokes mostly containing *tāli*-sam-s and *tāli*-vibhāga boundaries having bayan-component, for a polyphonic composition. In the Figure 7(2), the corresponding time positions of are shown.
- However, there would always be some noisy peak-s in $\{bp_j\}$, hence a further refinement is done as per the described method and finally the refined bayan-stroke-signal is shown in the Figure 7(3).

Peak-signal

From the input polyphonic signal waveform, differential envelope is generated after applying half-wave rectifier. The peak-s is extracted from the amplitude envelope of the signal, by calculating the local maxima-s. Local maxima-s are defined as the peak-s in the envelope with amplitude higher than their adjoining local minima-s by a default threshold quantity of $d_f \times I_{max}$, where I_{max} , is the maximum amplitude point of the envelope. Here we have taken default minimum value for d_f in the MIR toolbox [43], which would extract almost all the peak-s in the input envelope. Each peak in the peak-signal is mainly generated out of *tablā* and other percussive instruments played in the polyphonic composition. These peak-s are supposed to be more stressed than other melodic instruments and vocals rendered with comparatively more steady range of energies (without much ups and down, hence unable to produce high-energy peak-s). Figure 8 (1) shows all the peak-s along with the positions of the bayan-strokes of the bayan-stroke-signal in bold, for the same test clip of the Figure 7. The bayan-stroke-signal has been generated as per process in section our approach.

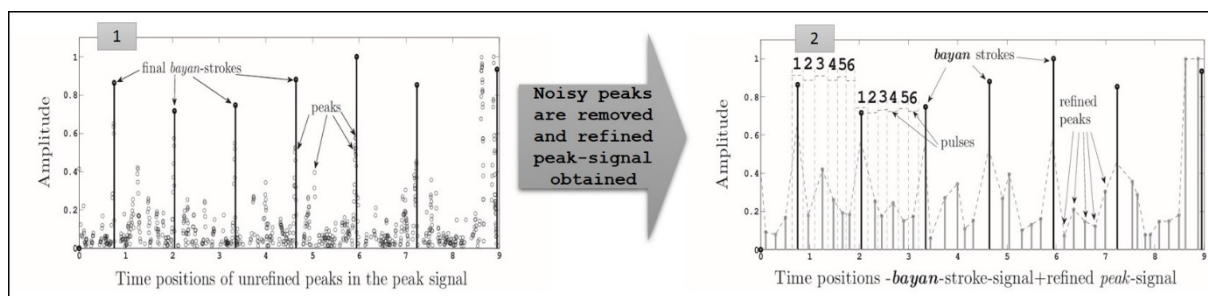


Figure 8: Percussive peak-s along with bayan-strokes in bold line, for a polyphonic clip of dadra *tāla*.

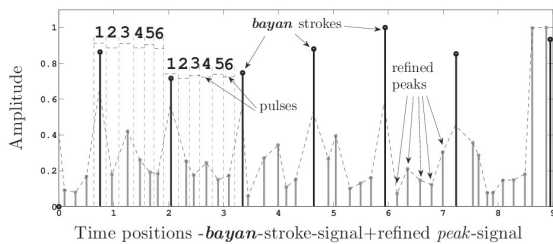


Figure 9: Magnified version of Figure 8.

Refinement of bayan and peak-signal

There may be multiple percussive instruments and also human voice in a polyphonic composition. There is a tendency to stress more at the *tāli-sam* and *tāli-vibhāga* boundaries by the performer, while singing along with the *tāla*. Hence for polyphonic compositions, other percussive instruments and human voice also generate peak-s in the bayan-stroke-signal, coinciding with bayan-strokes.

Peak-signal for polyphonic signal also consists of peak-s produced by *tablā*, percussive instruments (if present) and human voice. For both bayan-stroke and peak signals, these peak-s should coincide with respect to their positions in *X*-axis or time of their occurrences. But among them the peak-s generated out of *tablā* or the drum instrument here, are usually of higher strength. Using this theory we go for refinement of both bayan-stroke-signal and peak-signal to retain the most of the peak-s generated from *tablā*, and discard other kinds of percussive peak-s. It has been observed that most of the popular Hindi compositions (classical or semi-classical) have tempo much less than 600 beats per minute [Rhythm Taal]. Thereby minimum beat interval or gap between consecutive *tablā* strokes in these compositions, is much more than $60/600=0.1$ sec.

Hence both the bayan-stroke-signal and peak-signal are divided into 0.1 sec duration windows along *X*-axis. For each window the peak having highest strength is retained as correct bayan-stroke (in bayan-stroke-signal) or any other valid *tablā* peak (in peak-signal), and rest of the peak-s in each window is dropped. This way the noisy peak-s is removed and final bayan-stroke-signal and peak-signal are obtained. Figure 8 (2) shows the final, high-strength and refined peak-signal, with the positions of the bayan-strokes of the refined bayan-stroke-signal in **bold**. The same final peak-signal is referred in Figure 7 (4). Figure 9 is the magnified version of Figure 8 (2) and Figure 7 (4).

Analysis based on *tablā* and *tāla* theory

The refined peak-signal for the same clip in *dadra tāla* is shown in Figure 9. As per the *thekā* of *dadra* in Table 3, apart from the *sam-dha* there is no other *tāla-vibhāga* boundaries, hence its final bayan-stroke-signal should contain these *sam-s* only.

- **Pulse:** Here pulse is defined as the amplitude envelope of a stroke whose peak is extracted in the peak-signal.
- **Peak:** It should be noted here that, a peak in the refined peak-signal, is the highest point of an amplitude envelope formed for a pulse. Hence peak is actually the mid-point of the pulse duration in seconds along the *X*-axis.

For the test clip of *dadra tāla*, the peak-s and the pulses are elaborated in Figure 9. Here we can see there are 5 peak-s and 6 pulses in between two consecutive bayan strokes.

The method of *tāla* detection based on *tablā* and *tāla* theory is explained in the following sections.

First level analysis of pulse pattern: As per the theories explained in section *Tāla* and its structure in NIMS and *Tablā* and *bol-s*, we have extended the Table 3 and created another Table 4. Here the first column describes number of probable pulses in between two bayan strokes, as per the theories. For example, for *dadra tāla*, number of pulses in between a *dha-bol/sam* of an *āvart* and the *dha-bol/sam* of the next *āvart* should theoretically be 6 as per the *dadra thekā* in the Table 4. This 6-6 pattern of number of pulses should continue along the progression of the composition. The third column describes the *thekā-s* corresponding to the pulse pattern, with *tāla-sam-s* and *tāli-vibhāga-boundary-bol-s* in bold as per the theory explained in section *Tāla* and its structure in NIMS and *Tablā* and *bol-s*. The pipes in bold represent the start of *vibhāga-boundaries* within single *āvart*. *āvart-sequences* are shown and for each *thekā*, a *āvart* and the starting *bol* of next *āvart* are given, to indicate the progression of *tāla-s*.

It is to be noted that *bhajani thekā* has half of its number of strokes as rests. Other percussive instrument and vocal emphasis would normally generate peak-s of moderate strength for the time positions of these strokes in an *āvart*, especially for the genres of our experimental compositions. Hence, here *bhajani* is considered as *tāla* with 16 pulses/*āvart*.

It should be noted that for *tāla-s* like *bhajani* and *rupak*, there are two sets of probable no of pulses. For example for *rupak* there is both 4-10 and 10-4. This is because we are calculating number of pulses for the consecutive *āvart* along the progression of the song. So suppose if we start from *āvart* 1, the second *vibhāga-boundary-bol* has bayan component and it will generate a peak in the bayan-stroke-signal. Next peak in the bayan-stroke-signal would be the third *vibhāga-boundary-bol*. So in between them (I dhin dhin dha dha I dhin) there would be 3 peak-s and 4 pulses. Next peak in the bayan-stroke-signal would be the second *vibhāga-boundary-bol* of the *āvart* 2 and evidently there would be 9 peak-s and 10 pulses between second and third peak-s in bayan-stroke-signal (dhin dhin dha dha 2 I tun na tun na ti te I dhin). It gives rise to pulse pattern of 4-10, considering first, second and third peak-s in bayan-stroke-signal. Now if we move on and consider second, third and fourth bayan-peak-s, the detected pulse pattern should be 10-4, then again 4-10 and it will go on for the entire progression of the

song. So both 4-10 and 10-4 would signify rupak tāla with same set of stressed bol-s in the thekā.

Table 4: Probable number of pulses in between consecutive bayan-strokes, corresponding thekā-s and the tāla-s.

Number of probable pulses between consecutive bayan-strokes āla-s	Tāla-s	Corresponding thekā-s with āvart-sequences
6-6	dadra	¹ dha dhi na na ti na ² dha..
8-8	kaharba	¹ dha ge na ti na ke dhi na ² dha..
4-10,10-4	rupak	¹ tun na tun na ti te dhin dhin dha dha dhin dhin dha dha ² tun na..
14-14	rupak	¹ tun na tun na ti te dhin dhin dha dha dhin dhin dha dha ² tun na..
3-13,13-3	bhajani	¹ dhin* na dhin*dhin na* tin*ta tin*tin ta* ² dhin* ..
16-16	bhajani	¹ dhin*na dhin*dhin na* tin*ta tin*tin ta* ² dhin* ..

Table 5: Probable number of pulses in between consecutive bayan strokes in the thekā for dadra tāla.

Number of probable pulses between consecutive bayan-strokes	Corresponding thekā-s with āvart-sequences
6-6	¹ dha dhi na na ti na ² dha..
1-5, 5-1	¹ dha dhi na na ti na ² dha dhi..

Extended analysis of pulse pattern: It should be noted that, in vilambit compositions there may be additional filler strokes apart from the basic thekā, which lead to additional significant peak-s in both the bayan-stroke-signal and the peak-signal. In druta compositions often several thekā strokes are skipped and only vibhāga-s are stressed.

Table 4 shows the elementary set of probable pulses in between consecutive bayan strokes for clear understanding of the concept. To keep room for variations and improvisations of the thekā that are allowed within a specific tāla, we have extended this set in our experiment. There we have included all the probable patterns of pulse-counts, by considering the probability of additional bayan or bayan+dayan -strokes in a thekā to be stressed. We are assuming that apart from the mandatory tāli-sam and tāli-vibhāga boundaries, any other bol-s having bayan component may be stressed and produce a peak in the bayan-stroke-signal.

Here we have shown all the probabilities (including basic and extended) for dadra tāla in Table 5, as an example. Here in this dadra-thekā apart from the tāli-sam-bol which is dha, of a āvart, the very next bol is dhi also has bayan-component. So apart from mandatory sam this bol can also be stressed and give rise to pulse pattern of 1-5, 5-1. Similarly for rest of the tāla-s, all probable combinations of number of pulses are calculated.

Generation of co-occurrence matrix and detection of tāla: For each test sample, we have taken the refined version of bayan-stroke-signal, peak-signal (generated and refined as per the method in above section) and the co-occurrence matrix is formed and tāla is detected as per the following steps. Here co-occurrence matrix displays the distribution of co-occurring

pulse-counts along the sequence of the bayan-stroke-intervals, in a matrix format The Figure 7 shows the overall process flow of generation of co-occurrence matrix from refined bayan-stroke-signal and peak-signal.

Table 6: Co-occurrence matrix formed for a composition played in dadra-tāla

	1	2	3	4	5	6	7	...
1	0	0	0	0	3*	0	0	...
2	0	0	0	0	0	0	0	...
3	0	0	0	0	0	0	0	...
5	0	0	0	0	0	0	0	...
6	0	0	0	0	0	10*	0	...
7	0	0	0	0	0	0	0	...
...

*Highlighted region

- We extract the time positions of the peak-s of the refined peak-signal and the bayan-stroke-signal along the X-axis or time axis.
- Then we calculate the count of peak-signal-pulses occurring in each of the time intervals formed by consecutive peak-s of bayan-stroke-signal. Here we denote the series of pulse-counts calculated for a test-sample as $(pc_1, pc_1... pc_k)$, where $k=(\text{number of bayan-strokes})$. For example, we can see in the Figure 9, there are 5 peak-s between two consecutive bayan-strokes the number of pulses are 6 or $pc_1=6$. Similarly, we calculate the rest of the pc_i -s.
- Then we form 16 x 16 co-occurrence matrix (having 16 rows and 16 columns/row) and initialize all of its elements with zero. Maximum dimension of the matrix is taken as 16 because for our test data there can be maximum of 16 numbers of pulses between consecutive bayan-strokes (Refer Table 4).
- Then we fill up the co-occurrence matrix by occurrence of each pair of pulse-counts between the consecutive intervals

in the bayan-stroke-signal formed for the whole test sample. We denote each consecutive pair as pc_i, pc_{i+1} where $pc_i \in (1, 2...16)$ and $pc_{i+1} \in (1, 2...16)$. For example if the number of pulses between first and the second peak-s in the bayan-stroke-signal is 4 and the same between the second and the third is 6. So pc_1, pc_2 becomes 4, 6 and we add 1 to the matrix element of fourth row and sixth column, which now becomes 1 from initialized zero value. Then we check the same between third and fourth peak which is suppose 6, hence pc_2, pc_3 , becomes 6, 6 and now 1 is added to the matrix element of sixth row and sixth column, making it 1 from zero.

- We traverse the whole peak-signal and the bayan-stroke-signal and update the matrix. Each cell of the matrix contain the occurrence of a particular pulse count pattern in consecutive intervals in bayan-stroke-signal.
- Finally we extract the row and column index of the cell in the matrix containing the maximum value. This row and column index is the most occurring pattern of pulse counts in consecutive intervals in bayan-stroke-signal. Here this row-column index of the matrix is denoted by $(pcmax_1, pcmax_2)$.
- The co-occurrence matrix for a test sample is shown in Table 6 where we can see 10 as the maximum value in 6th row and 6th column i.e. $(pcmax_1=6, pcmax_2=6)$.
- Then the $(pcmax_1, pcmax_2)$ is matched against the first column of the Table 4 and also the rules defined above. Accordingly tāla is decided from its second column. For the test sample for which the co-occurrence matrix is shown in the Table 6, $pcmax_1=6$ and $pcmax_2=6$ are extracted and it is exactly matched with 6-6 pattern for number of probable pulses between consecutive bayan-strokes, hence it is detected as of dadra tāla.
- While matching occurrence pattern of peak-s between consecutive bayan-peak-s, apart from the rules explained in section First level analysis of pulse pattern and extended analysis of pulse pattern, a tolerance of ± 1 considered. For example, if for a test clip we get 6-6 number of peak-s between consecutive bayan duration in the bayan-stroke-signal, we detect it as of dadra tāla. But even if we get 6-5 or 5-6, then also detect it as dadra. This way we are considering human errors within a narrow range of tolerance.

Detection of tempo: Tempo or lay is detected in terms of pulses per minute as per the method below.

- Once we detect $(pcmax_1, pcmax_2)$ we get the tāla as per the process described earlier. Then we collect all the consecutive pair of bayan durations having $pcmax_1$ and $pcmax_2$ number of pulses for the whole composition. In the Figure 9, we can see that for this particular dadra clip there are 6 number of pulses in the intervals between first two bayan-strokes and also second, third bayan-strokes.
- Suppose these bayan durations are denoted by $(bd1_1, bd1_2...bd1_n)$ having $pcmax_1$ number of pulses and $(bd2_1, bd2_2...bd2_n)$ having $pcmax_2$ number of pulses, where n is the value in the cell of co-occurrence matrix having row index $pcmax_1$ and column index $pcmax_2$. It basically means that $(pcmax_1, pcmax_2)$ pair has occurred for n no of times in the co-occurrence matrix and also in the whole test composition.

- Then all these bayan durations are added. We denote that by

$$bayan_{dur} = \sum_{i=1}^n bd1_i + \sum_{i=1}^n bd2_i. \text{ Total number of pulses in these durations are } count_{pulse} = n * (pcmax_1 + pcmax_2). \text{ } bayan_{dur} \text{ is measured in second. The average duration of a pulse in the composition is calculated as } pulse_{dur} = \frac{bayan_{dur}}{count_{pulse}} \text{ in second. Then the tempo is calculated as } tempo = \frac{60}{pulse_{dur}} \text{ in beats per minute.}$$

Experimental details

Data description

We have experimented with a number of polyphonic compositions of NIMS vocal songs rendered with four popular theka-s of the tāla-s, as described in Table 4. The test compositions are from bhajan or devotional, semi-classical and film-music genres, having tablā and other percussive instruments as accompaniments. The film-music and semi-classical genres are chosen because they mostly maintain similar structures with minimal improvisation and regular tempos as far as rhythm of the compositions are concerned. Hence this test dataset should be suitable for finalizing the elementary layer of the tāla-detection system of NIMS.

The tāla-s considered are dadra, kaharba, rupak, bhajani, as most of the songs in above genres are composed in these tāla-s. Also we got maximum number of annotated samples of polyphonic songs composed with these tāla-s, which helped in rigorous testing and validation process. Also as these tāla-s have unique mātra-s and they would produce mostly unique number of peak-s between consecutive bayan-strokes, so experimenting with sufficient number of test samples composed in these tāla-s enabled us to validate the applicability of the initial version of our model.

The annotated list of tāla-wise songs are obtained from Sound of India and FILM SONGS IN VARIOUS TALS and also from the albums The Best Of Anup Jalota (Universal Music India Pvt Ltd), Bhanjanjali vol 2 (Venus), Bhajans (Universal Music India Pvt Ltd), Songs Of The Seasons Vol (Shobha Gurtu). The annotations are validated by renowned musician Subhranil Sarkar. All the song clips are in single channel .wav format sampled at 44100Hz and are annotated. The clips are of 60 second duration. The tempo ranges from madhya to ati-druta tempo. The tempo of the input samples were calculated by manual tapping by expert musicians and this calculated tempo were assumed to be our benchmark for validation. The detailed description of the data used is shown in Table 7. The tempo is uniformly maintained for the input sound samples of the experiment. The data reflects variation in terms of genre, types of instruments and voices in the composition, tempo and mātrā of the compositions.

Table 7: Description of data.

ta ⁻ la	ma ⁻ tra ⁻	Tempo range (in BPM)	No of clips
dadra	6	140-320	65
kaharba	8	220-400	65
bhajani	8	300-360	65
rupak	7	240-375	65

Results

Table 8: Confusion matrix for tāla detection for the clips (all figures in %).

	dadra	kaharba	bhajani	rupak	none
dadra	80.85	6.38	6.38	4.26	2.13
kaharba	4.17	81.25	8.33	2.08	4.16
bhajani	3.57	12.5	78.57	3.57	1.79
rupak	3.5	4.5	4	86	2

Table 8 shows the confusion matrix for tāla detection. Here the column none signifies that the tāla of the input clip is NOT detected as any of the input tāla-s (dadra, kaharba, rupak, bhajani). There is an incorrect detection between the pair of kaharba and bhajani. Few bhajani samples have been detected as kaharba and vice-versa. For a specific laggi or variation of bhajani tāla Bhajan taal, a composition might turn out to be with 8-8 pulse pattern where $[pcmax_1=8, pcmax_2=8]$. In this case it would be detected as kaharba as per our method. However, this error is not so severe as technically bhajani is a variation of kaharba [8].

Also as per the Table 4 theoretically 8-8 pulse pattern is for kaharba and 16-16 is for bhajani, i.e. pattern for bhajani is exactly twice of kaharba. For some rare cases of manual error, while playing tablā in kaharba, the tablā-expert might make some sam-s less stressed and this sam-s might fail to generate bayan-peak-s in the refined bayan-stroke-signal. In these cases kaharba might produce 16-16 pulse pattern and would be detected as bhajani. However, this is much rare as theoretically for any tablā composition the tāli-bol-sam must be stressed.

Table 9 shows the performance of proposed methodology in detecting tempo for different compositions. In judging the correctness of tempo, a tolerance of $\pm 5\%$ is considered.

Table 9: Performance of tempo detection (all figures in %).

Ta ⁻ la	Correct detection
dadra	80.85
kaharba	77.08
bhajani	80.35
rupak	76

Overall tāla and tempo detection performance is shown in Table 10 Gross performance of tāla and tempo detection (all

figures in %). It is clear that the proposed methodology performs satisfactorily and that too with wide variety of data.

Table 10: Gross performance of tāla and tempo detection (all figures in %).

Average performance	
ma ⁻ tra ⁻ detection	Tempo detection
81.59	78.6

Conclusion

- This paper presents the results of analysis of tablā signal of North Indian polyphonic composition, with the help of new technique by extracting the bayan signal.
- The justification of using bayan signal as the guiding signal in case of North Indian polyphonic music and detecting tāla using the parameters of NIMS rhythm, has been clearly discussed.
- A large number of polyphonic music samples from Hindi vocal songs from bhajan or devotional, semi-classical and filmy genres were analyzed for studying the effectiveness of the proposed new method.
- The experimental result of the present investigation clearly supports the pronounced effectiveness of the proposed technique.
- We would extend this methodology for studying other features (both stationary and non-stationary) of the all the relevant tāla-s of NIMS and designing an automated rhythm-wise categorization system for polyphonic compositions. This system may be used for content-based music retrieval in NIMS. Also a potential tool in the area of music research and training is expected to come out of it.
- Limitations of the method are that it cannot distinguish between tāla-s of same mātra. For example deepchandi and dhamar tāla-s have number of mātra -s, bol-s and beats in a cycle. We plan to extend this elementary model of tāla-detection system for all the NIMS tāla-s, by including other properties like timbral information and nonlinear properties of different kinds of tablā strokes/bol-s. We may also attempt to transcript the tāla-bol-s in a polyphonic composition. This extended version of the model may address the NIMS tāla-s which share same mātra and also have variety of lay-s.

The initial version of the software version of the proposed algorithm is in Talman, where users can upload relevant .wav files of a polyphonic song played on NIMS tāla-s and find out the tāla computationally.

Acknowledgement

We thank the Department of Higher Education and Rabindra Bharati University, Govt. of West Bengal, India for logistics support of computational analysis. We also thank renowned musician Subhranil Sarkar for helping us to annotate test data, validate test results and Shiraz Ray (Deepa Ghosh Research

Foundation) for extending help in editing the manuscript to enhance its understandability.

References

1. London J (2004) *Hearing in Time*. Oxford University Press.
2. Cooper GW, Meyer LB (1960) The rhythmic structure of music.
3. Lerdahl F, Jackendoff RS (1985) *A Generative Theory of Tonal Music*. Cambridge, Mass.: MIT Press Ltd, p. 384.
4. Latham A (2011) *The Oxford Companion to Music*. Oxford University Press.
5. Gillet O, Richard G (2005) Extraction And Remixing Of Drum Tracks From Polyphonic Music Signals, in *Applications of Signal Processing to Audio and Acoustics*. IEEE Workshop, pp. 315-318.
6. Ono N, Miyamoto K, Roux JL, Kameoka H, Sagayama S (2008) Separation of a monaural audio signal into harmonic/percussive components by complementary diffusion on spectrogram, in *Proc. of the EUSICO European Signal Processing Conf.*
7. Clayton M (2000) *Time in Indian Music?: Rhythm , Metre and Form in North Indian Rag Performance*. Oxford University Press.
8. Courtney DR (2000) *Fundamentals of Tabla*. (4th editn) Sur Sangeet Services, pp. 294.
9. Nainpalli S (2005) *The theory and Practice of TABLA*. Popular Prakashan, Mumbai, India, pp. 250.
10. Alghoniemy M, Tewfik AH (1999) Rhythm and periodicity detection in polyphonic music. In: *IEEE Third Workshop on Multimedia Signal Processing*. IEEE, pp. 185-190.
11. Rosenthal D (1992) Emulation of Human Rhythm Perception. *Comp Music J* 16: 64-76.
12. Bakhmutova IV, Gusev VD, Titkova TN (1997) The Search for Adaptations in Song Melodies. *Comp Music J* 21: 58-67.
13. Todd NPM, Brown GJ (1996) Visualization of Rhythm, Time and Meters. *Art Intel Rev* 10: 99-119.
14. Foote J (2000) Automatic audio segmentation using a measure of audio novelty. *IEEE International Conference on Multimedia and Expo, Tokyo, Japan*, pp. 452-455.
15. Klapuri AP, Eronen AJ, Astola JT (2006) Analysis of the meter of acoustic musical signals. *IEEE Trans Audio Speech Lang Proc* 14: 342-355.
16. Gouyon F, Herrera P (2003) Determination of the meter of musical audio signals: Seeking recurrences in beat segment descriptors, *114th Audio Engineering Society Convention Spain*, pp. 5811
17. Bhat R (1991) Acoustics of a cavity-backed membrane: The Indian musical drum. *J Acous Soc Ame* 90: 1469-1474.
18. Goto M, Muraoka Y (1995) A real-time beat tracking system for audio signals. In *Proc. International Computer Music Conference Japan*, pp. 311-335
19. Scheirer ED (1998) Tempo and beat analysis of acoustic musical signals. *J Acoust Soc Am* 103: 588-601.
20. Gouyon F, Herrera P (2001) Exploration of techniques for automatic labeling of audio drum tracks instruments. *Curr Direct Comp Music*.
21. Dixon S (2007) Evaluation of The Audio Beat Tracking System BeatRoot. *J New Music Res* 36: 39-50.
22. Davies MEP, Plumbley MD (2007) Context-dependent beat tracking of Musical Audio. *IEEE Trans Audio Speech Lang Proc* 15: 1009-1020.
23. Böck S, Schedl M (2011) Enhanced Beat Tracking with Context-aware Neural Networks. *Proc 14th Int Conf Digital Audio Effects* pp. 135-139.
24. Raman CV (1921) On some Indian stringed instruments. *Proc Indian Assoc Cultiv Sci* 33: 29-33.
25. Malu S, Siddharthan A (2000) Acoustics of the Indian drum. *ArXiv Preprint Math* 1-13.
26. Patel A D, Iversen JR (2003) Acoustic and Perceptual Comparison of Speech and Drum Sounds in the North Indian Tabla Tradition: An Empirical Study of Sound Symbolism. *15th ICPhS Barcelona*, pp. 925-928.
27. Rae A (2009) *Generative Rhythmic Models*.
28. Gulati S, Rao V, Rao P (2011) Meter detection from audio for Indian music in *Proc. Int. Symposium on Computer Music Modeling and Retrieval* pp. 34-43.
29. Schuller B, Eyben F, Rigoll G (2007) Fast and Robust Meter and Tempo Recognition for the Automatic Discrimination of Ballroom Dance Styles. In *Acoustics, Speech and Signal Processing, 2007 IEEE International Conference* pp 217-220.
30. Miron M (2011) Automatic Detection of Hindustani Talas.
31. Bhaduri S, Saha SK, Mazumdar C (2014) Matra and Tempo Detection for INDIC Tala-s. *Adv Com Inf, Proceedings of the Second International Conference on Advanced Computing, Networking and Informatics* 1: 213-220.
32. Bhaduri S, Saha SK, Mazumdar C (2014) A Novel Method for Tempo Detection of INDIC Tala-s. *Fourth Int Conf Emerg App Inf Tech* 222-227.
33. Bhaduri S, Das O, Saha SK, Mazumdar C (2015) Rhythm analysis of tabla signal by detecting the cyclic pattern. *Innovations Syst Softw Eng* 11:187-195.
34. Maity A, Pratihari R, Mitra A, Dey S, Agrawal V et al (2015) Multifractal Detrended Fluctuation Analysis of alpha and theta EEG rhythms with musical stimuli. *Chaos Solitons Fractals* 81: 52-67.
35. Clayton M (1997) The meter and the tāl in the music of north india. *Tradit Music* 10: 169-189.
36. Uhle C, Dittmar C, Sporer T (2003) Extraction of drum tracks from polyphonic music using Independent Subspace Analysis. In *Proceedings of the 4th International Symposium on Independent Component Analysis and Blind Signal Separation*, pp. 843-848.
37. Helen M, Virtanen T (2005) Separation of drums from polyphonic music using non-negative matrix factorization and support vector machine. *Proc. Eur Signal Process Conf.*
38. Zils A, Pachet F, Delerue O, Gouyon F (2002) Automatic extraction of drum tracks from polyphonic music signals. *Web Delivering of Music, WEDELMUSIC, Proceedings Second International Conference*, pp. 179-183.
39. Yoshii K, Goto M, Okuno HG (2004) Automatic drum sound description for real-world music using template adaptation and matching methods. In *Proceedings of the International Conference on Music Information Retrieval*, pp. 184-191.
40. Gillet O, Richard G (2003) Automatic Labelling of Tabla Signals. In *Proc. ISMIR*.

41. Moore BCJ, Glasberg BR (1983) Suggested formulae for calculating auditory-filter bandwidths and excitation patterns. *The J Aco Soc Ame* 74: 750-753.
42. Ranade SG (1964) Frequency spectra of Indian music and musical instruments. Research Department, All India Radio, New Delhi.
43. Lartillot O, Toiviainen P (2007) A matlab toolbox for musical feature extraction from audio. *International Conference on Digital Audio*. pp. 1-8.